

## Motivation

Q1: Should pseudo-anomalies approximate the queries in test phase?

- There is no clear definition of what constitutes an anomaly, there shouldn't be any bound or limit on pseudo anomaly.
- We advocate generating a diversity of anomalies to facilitate a model to learn the comprehensive normal spectrum, instead of matching known abnormal patterns.

Q2: How should the segmentation model be trained on the synthesis data?

- A covariate shift is likely to exist between the synthesized and real anomalies, according to Fig 1(C). Good-fit models on the pseudo-anomalies may fail to detect real anomalies.
- The model optimization on anomaly synthesis for pseudo-supervised segmentation should stop early to preserve the model's generalizability on queries.

## Method

We adopted the DREAM[1] architecture and incorporated three key elements: random-shape anomaly generation, two-phase learning mechanism, and UNet reconstruction network.

### Random-shape Anomaly Generation

**Algorithm 1** Random-shape Pseudo Anomaly Generation

**Input:**  $Image, Threshold$

**Output:**  $AnomalyMask, Label$

```

NoiseImage ← gaussianNoise(Image.height, Image.width)
BlurImage ← gaussianBlur(NoiseImage, kernel_size)
StretchImage ← rescaleIntensity(BlurImage, (0, 255))
AnomalyMask ← binarize(StretchImage, Threshold)
AnomalyMask ← Morph_open_close(AnomalyMask, kernel_ellipse)
if sum(AnomalyMask) > 0 then
    Label ← 1
else
    Label ← 0
end if
    
```

The pseudo anomaly synthesis is shown in Fig. 1(B) and formulated as:

$$I_s = (1 - M_s) \odot (I + C) + M_s \odot I, \quad |C| \in (minRange, maxRange)$$

where  $I_s$  represents synthesized anomalies,  $\odot$  is the element-wise multiplication, and  $C$  is randomly drawn from a Gaussian distribution within a defined range

### Two-stage Training Strategy

Due to the covariate shift of the synthesized anomalies, we observed high perturbations in evaluation performance, therefore, we propose to train the networks in two steps: As Depicted in Fig. 2(A), the reconstruction network is trained to restore anomalous regions, while the segmentation network estimates an accurate segmentation map for the anomaly.

- The reconstruction model is first trained with  $L_1$  loss:

$$L_{rec}(I_s - \tilde{I}_s) = |I_s - \tilde{I}_s|$$

- After freezing the well-trained generative module, Focal Loss [2] is adopted to slightly train the segmentation model to avoid bias introduced by the covariance shift, :

$$L_{seg}(M_s - \tilde{M}_s) = -\frac{1}{N} \sum_{i=1}^N \sum_{j=1}^C \alpha_j (1 - \tilde{m}_{s,ij})^{\gamma} \log(\tilde{m}_{s,ij})$$

where  $\tilde{I}_s$  is the reconstruction image,  $\tilde{M}_s$  is the estimated anomaly mask,  $\tilde{m}_{s,ij}$  denotes the predicted probability of class  $j$  at pixel  $i$ , and  $\alpha_j$  is the weight for class  $j$ .

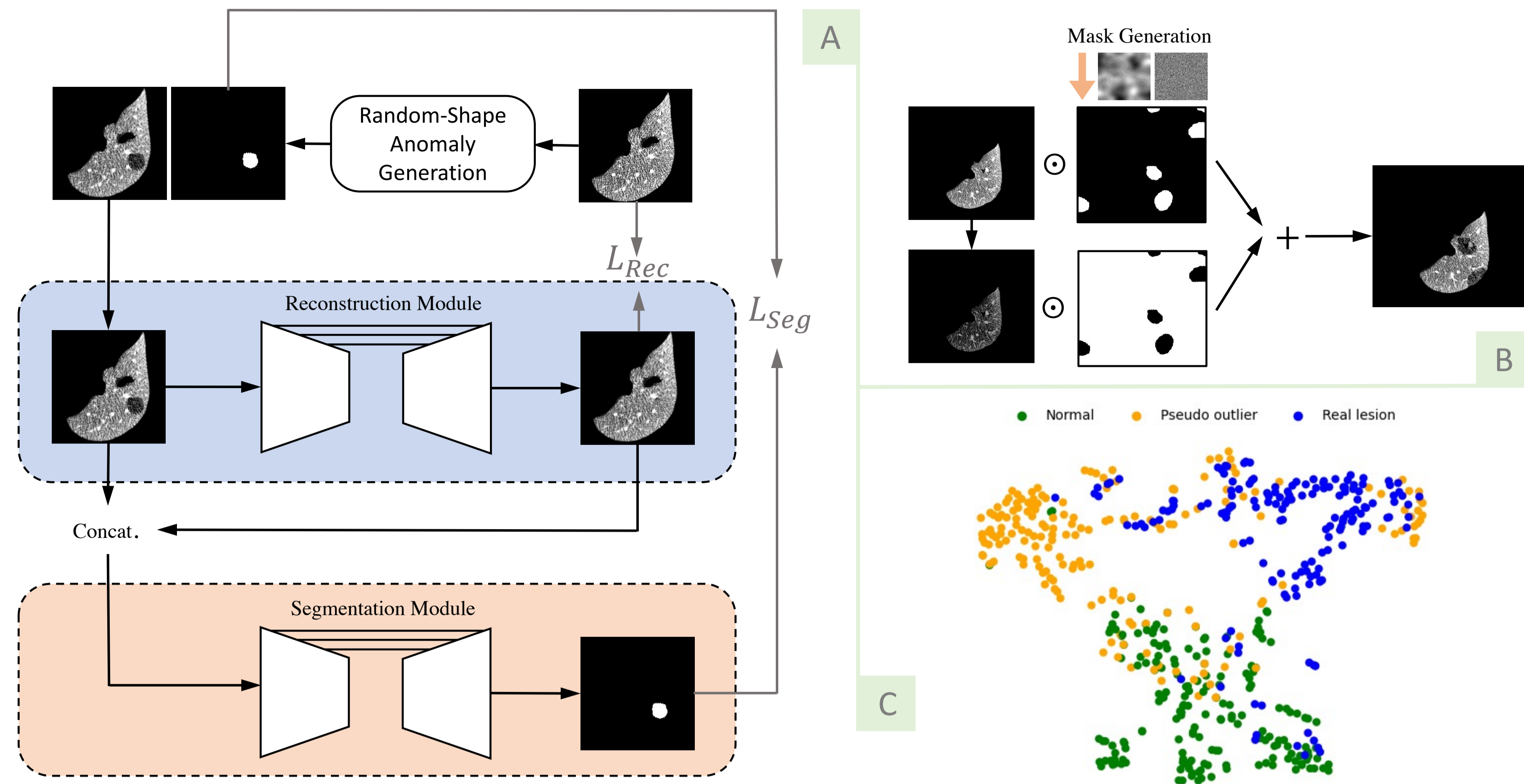


Fig. 1. (A) Systematic diagram of the proposed unsupervised liver tumor segmentation scheme. During training, synthetic abnormalities are fed to a restoration net followed by a segmentation net. The two models are trained in two phases to avoid model overfitting on synthesis. (B) Proposed synthesis pipeline based on Gaussian noise stretching. (C) Liver image embedding by 2-D TSNE.

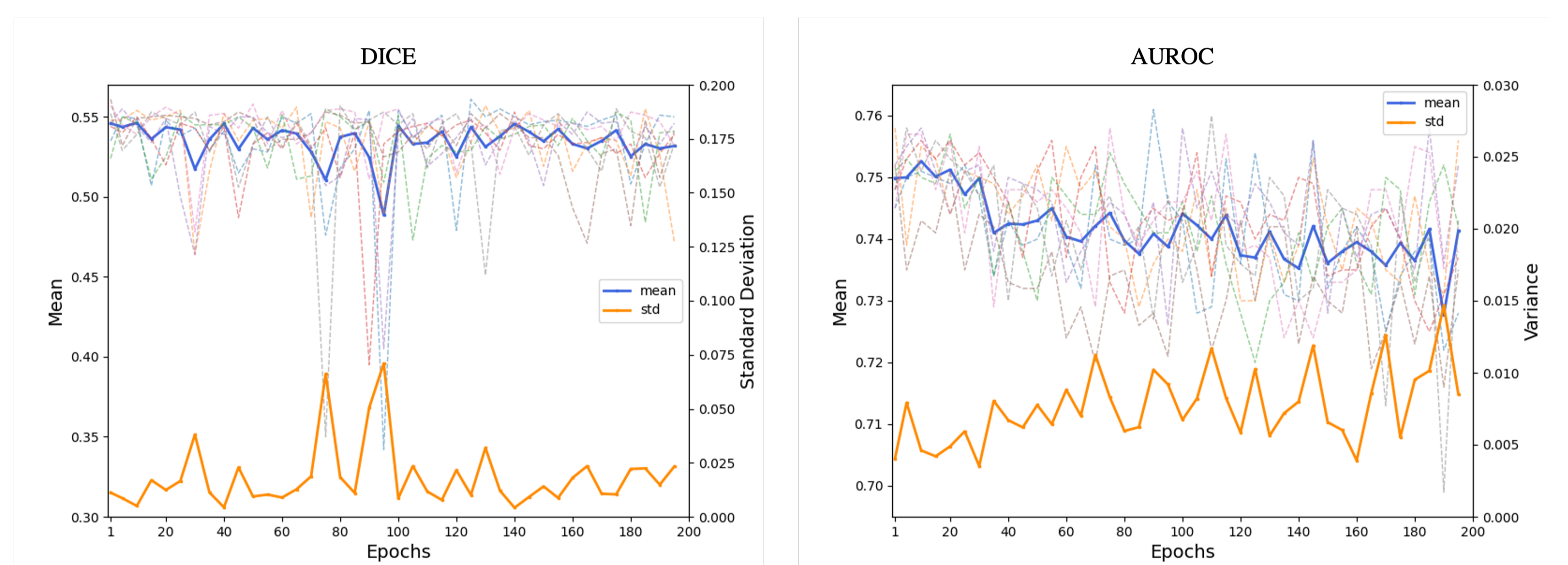


Fig. 2. Evaluation performance of the segmentation network reveals a tendency to overfit shortly after a short period of training.

## Results

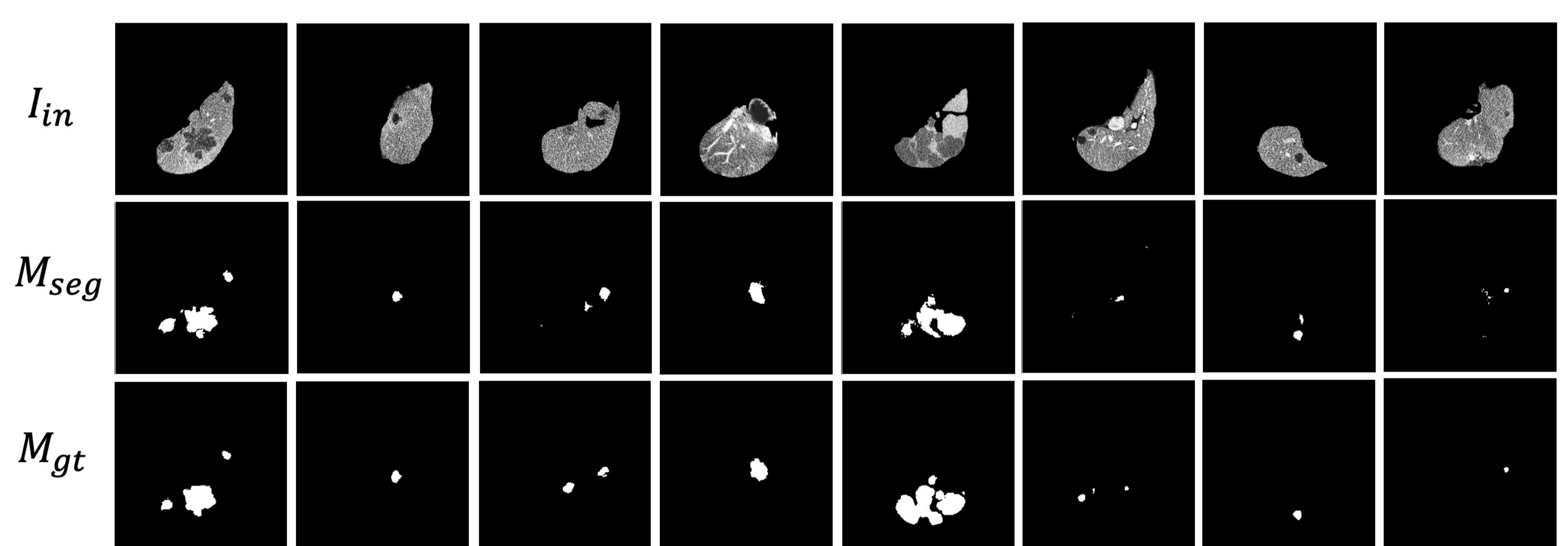


Fig. 3. Qualitative results of tumor segmentation on real liver tumor data.  $I_{in}$ : Input,  $M_{seg}$ : segmentation mask, and  $M_{gt}$ : Ground-Truth.

Table 1. Ablation study of two-phase training (TP), pseudo anomaly (PA), and reconstructive network. The baseline is DRAEM model [1].

	+TP	+PA	+UNet	Dice
				14.75 ± 14.28
	✓			21.31 ± 12.54
	✓	✓		30.17 ± 5.50
		✓	✓	40.06 ± 6.85
<b>Base line</b>	✓	✓	✓	<b>53.03 ± 1.78</b>